

Noncoherent Reconfigurable Intelligent Surface With Differential Modulation and Reflection Pattern Training

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Abstract—In this paper, we propose a novel noncoherent reconfigurable intelligent surface (RIS)-assisted downlink architecture aided by lightweight reflection pattern training as well as noncoherent detection. More specifically, the proposed scheme amalgamates the benefits of reflection pattern training and differential modulation, which operate without any channel estimation in each stage of RIS optimization and data detection, hence combating the delay-induced limitations. The proposed scheme achieves low training complexity and robustness over the channel variation in comparison to the conventional RIS optimization assuming the use of channel state information. We demonstrate that the proposed scheme outperforms the conventional coherent benchmarks.

Index Terms—noncoherent detection, overhead reduction, pattern training, reconfigurable intelligent surface, training.

I. INTRODUCTION

Reconfigurable intelligent surface (RIS) has the exclusive benefits of low-cost passive reflection as a virtual relay node [1–3]. Since millimeter-wave communication suffers from the blockage of an obstacle due to its high path loss and low refraction capability, the RIS technology may be a promising solution to extend the coverage in a reliable manner. By contrast, one of the most challenging issues for the practical RIS operation is the substantial overhead needed for controlling the RIS elements as well as the associated increased communication latency [3–5]. To achieve optimal phase shifts of each RIS element, perfect channel state information (CSI) between a base station (BS) and the RIS, as well as that between the RIS and a user, is needed in addition to complicated non-convex optimization based on the acquired CSI. Furthermore, the CSI estimation with pilot transmissions, as well as the non-convex optimization, has to be completed sufficiently faster than channel coherence time. Note that the associated overhead and latency increase upon increasing the number of RIS elements.

In order to relax the limitations imposed by channel estimation and non-convex optimization, several beam-training schemes were proposed for reducing overhead imposed by an RIS control [6–8]. In [7], hierarchical training was proposed,

where wide and narrow beam sectors are selected in order. Also, in [8], the complexity imposed by RIS training is reduced with the aid of a multi-mode grouping method that supports moderate combining gain. Alternatively, random RIS beamforming [9] allows us to dispense with CSI knowledge, although the full RIS beamforming gain is unachievable. More recently, in [10, 11], the RIS that is controlled by the pulse width of an incoming wave is proposed to remove the control voltage lines to each RIS element and symbol-level synchronization between the BS and the RIS.

While the majority of the previous RIS studies assumed the coherent detection at the receiver, several RIS-assisted systems employed noncoherent detection [12–14], in order to dispense with the channel estimation and reduce the pilot overhead. In [12], the combination of differential modulation and permutation modulation is exploited at the RIS for a downlink scenario, and the receiver is allowed to detect the signal in a noncoherent manner. In [14], RIS-aided noncoherent OFDM uplink is considered, where differential modulation is employed at an uplink user while RIS relies on random phase reflection at each element. However, the previous noncoherent RIS schemes, such as [12–14], sacrifice the beneficial beamforming gain since associated CSI is unavailable to dispense with channel estimation. More recently, in [15], the combination of differential modulation at a user and beam training of RIS is proposed for an RIS-assisted uplink system, although the presence of the direct user-to-BS link is assumed.¹

Against the above-mentioned background, the novel contribution of this paper is that we propose the noncoherent RIS-assisted downlink architecture in the absence of an idealistic direct BS-to-user link, in order to dispense with channel estimation for both RIS optimization and data detection.² More specifically, the proposed scheme amalgamates the benefits of differential modulation and pattern training, which operate without any channel estimation. The proposed scheme achieves low training complexity and robustness over the channel variation. We demonstrate the performance analysis of the proposed scheme in comparison to the conventional coherent counterpart.

The remainder of this paper is organized as follows. In Section II, we introduce the system model of our RIS-assisted noncoherent communication system. In Section III, our simulation results of the achievable BER performance are provided. Finally, in Section IV, this paper is concluded.

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¹Most recently, in [16], the tradeoff between the outdatedness of CSI and the system performance is characterized by the effective capacity. Furthermore, in [17], pilot overhead for estimation of uplink cascaded channel is reduced in a sub-6-GHz scenario.

²In a millimeter-wave scenario, an RIS is typically expected to combat the detrimental non-line-of-sight scenario (NLOS) while RIS does not have to be activated in the presence of a stable direct link.

while we have

$$\psi_B^t = \frac{2d_B}{\lambda} \cos \vartheta \cos \varphi \quad (11)$$

$$\psi_{R,x}^r = \frac{2d_x^R}{\lambda} \cos \theta^r \cos \phi^r \quad (12)$$

$$\psi_{R,z}^r = \frac{2d_z^R}{\lambda} \sin \phi^r \quad (13)$$

$$\psi_{R,x}^t = \frac{2d_x^R}{\lambda} \cos \theta^t \cos \phi^t \quad (14)$$

$$\psi_{R,z}^t = \frac{2d_z^R}{\lambda} \sin \phi^t. \quad (15)$$

Also, λ represents the wavelength.

We assume that the BS and the RIS remain unmoved, and the LOS component associated with the channel between them is considered quasi-static. Hence, the beam at the BS is fixed toward RIS to maximize the received LOS component at the RIS by setting the antenna weights to be $\mathbf{w} = \sqrt{P_t/M} \mathbf{a}_B^*(\vartheta, \varphi)$.

Furthermore, the fixed BS weights allow us to simplify the cascaded channel as follows. First, let us define the LOS component of the cascaded channel \bar{c}_i as

$$\bar{c}_i = \eta \bar{\mathbf{h}}_i^T \mathbf{\Omega} \bar{\mathbf{G}} \mathbf{w}, \quad (16)$$

where

$$\eta = \sqrt{\frac{L_{BR} \kappa_{BR}}{(\kappa_{BR} + 1)}} \sqrt{\frac{L_{RU} \kappa_{RU}}{(\kappa_{RU} + 1)}}. \quad (17)$$

Also, in the rest of this paper, $\mathbf{u}(\psi_{R,x}^t, N_x)$ and $\mathbf{u}(\psi_{R,z}^t, N_z)$ are simply expressed as $\mathbf{u}(\psi_{R,x}^t)$ and $\mathbf{u}(\psi_{R,z}^t)$, respectively. Then, \bar{c}_i is represented by [6]

$$\bar{c}_i = \eta \bar{\mathbf{h}}_i^T \mathbf{\Omega} \bar{\mathbf{G}} \mathbf{w} \quad (18)$$

$$= \eta \sqrt{P_t/M} \bar{\mathbf{h}}_i^T \mathbf{\Omega} (\mathbf{a}_B^H(\vartheta, \varphi) \mathbf{a}_B(\vartheta, \varphi)) \mathbf{a}_R(\theta^r, \phi^r) \quad (19)$$

$$= \lambda_i \sqrt{P_t M} \mathbf{b}_R^T(\theta^t, \phi^t) \mathbf{\Omega} \mathbf{a}_R(\theta^r, \phi^r)$$

$$= \lambda_i \sqrt{P_t M} (\mathbf{u}(\psi_{R,x}^t) \otimes \mathbf{u}(\psi_{R,z}^t)) \odot (\mathbf{u}(\psi_{R,x}^r) \otimes \mathbf{u}(\psi_{R,z}^r)) \mathbf{\omega}$$

$$= \lambda_i \sqrt{P_t M} (\mathbf{v}_x^T \otimes \mathbf{v}_z^T) \mathbf{\omega}, \quad (20)$$

where

$$\lambda_i = \exp(j2\pi i f_d \cos \theta_t) \eta \quad (21)$$

$$\mathbf{v}_x = \mathbf{u}(\psi_{R,x}^t) \odot \mathbf{u}(\psi_{R,x}^r) \quad (22)$$

$$\mathbf{v}_z = \mathbf{u}(\psi_{R,z}^t) \odot \mathbf{u}(\psi_{R,z}^r), \quad (23)$$

and \odot denotes the Hadamard product.

According to [6], the constraint of $\mathbf{\omega} = \mathbf{\omega}_x \otimes \mathbf{\omega}_z$ is imposed, where $\mathbf{\omega}_x \in \mathbb{C}^{N_x}$ and $\mathbf{\omega}_z \in \mathbb{C}^{N_z}$ are decomposed RIS's array steering vectors in the x axis and in the z axis, respectively. Then, (20) is rewritten by

$$\bar{c}_i = \lambda_i \sqrt{P_t M} (\mathbf{v}_x^T \otimes \mathbf{v}_z^T) (\mathbf{\omega}_x \otimes \mathbf{\omega}_z) \quad (24)$$

$$= \lambda_i \sqrt{P_t M} (\mathbf{v}_x^T \mathbf{\omega}_x) (\mathbf{v}_z^T \mathbf{\omega}_z) \quad (25)$$

By setting $\mathbf{\omega}_x = \mathbf{v}_x^* / \|\mathbf{v}_x\|$ and $\mathbf{\omega}_z = \mathbf{v}_z^* / \|\mathbf{v}_z\|$, $|\bar{c}_i|$ is maximized to $\eta \sqrt{P_t M} \|\mathbf{v}_x\| \|\mathbf{v}_z\|$. As shown in (25), the trained horizontal (x -axis) and vertical (z -axis) RIS patterns are decoupled. Hence, by assuming that $\phi^t = 0$ is set and known by the BS, we can focus our attention on the horizontal-

pattern training, similar to [6].

B. Reflection Pattern Training

Our RIS optimization consists of two steps, i.e., offline pattern design and online pattern training. More specifically, we prepare T RIS reflection patterns offline, i.e., in advance of transmissions. A minimum correlation of each pattern pair is minimized under the condition that minimum reflection gain to all reflected directions is kept higher than a specific threshold. Note that employing a low T value results in broad patterns.

In the proposed reflection pattern training scheme, one out of T RIS reflection patterns is selected. More specifically, the BS periodically transmits T reference symbols to the UE via the RIS while changing the reflection patterns of the RIS in each symbol interval. Then, based on feedback information, the BS finally determines the best reflection pattern that achieves the highest received power at the UE.

The conventional narrow-beam training of the RIS reflection coefficients training, which is based on exhaustive search, requires high pilot overhead, depending on the beam resolution [19]. Since the RIS is typically equipped with a large number of reflective elements, i.e., $N \gg 1$, the training overhead of the exhaustive search becomes significantly high. In order to circumvent this limitation, our proposed scheme exploits wide beam training with low training overhead $T \ll N$ at the expense of the reduction in the received power at the user.

More specifically, the i th RIS reflection pattern ($1 \leq i \leq T$) is designed for configuring a beam covering $\theta^t \in [\pi(i-1)/T, \pi i/T]$.

C. Differential Modulation and Noncoherent Detection

Having attained the BS weights and the RIS reflection coefficients above, now data transmission employing differential modulation at the BS is introduced. This allows us to eliminate CSI estimation at the user not only at the optimization stage of the RIS coefficients but also for data detection. At the BS, information bits are modulated onto the phase-shift keying (PSK) symbols s_t ($t \geq 1$), which are then differentially modulated as follows: [20]

$$x_t = \begin{cases} s_0 & t = 1 \\ x_{t-1} s_{t-1} & t \geq 2 \end{cases}, \quad (26)$$

where s_0 is a reference symbol transmitted at the beginning of data transmission.

From (26) and (3), we obtain

$$y_{i+1} = y_i s_i + n_{i+1} - n_i s_i \quad (i \geq 1), \quad (27)$$

under the assumption that the cascaded channel remains unchanged over the intervals of two symbols. Finally, the information symbols are detected based on the maximum likelihood detection as follows:

$$\hat{s}_i = \arg \min_{\forall s} |y_{i+1} - y_i s|^2 \quad (i \geq 1). \quad (28)$$

D. Overhead and Complexity Analysis

In this section, we characterize the pilot overhead and the complexity imposed for calculating the RIS coefficients

TABLE I
COMPARISONS OF PILOT OVERHEAD AND RIS OPTIMIZATION
COMPLEXITY BETWEEN THE PROPOSED AND BENCHMARK SCHEMES

	Pilot overhead and delay per coherent time	Complexity
Proposed training- based algorithm	$\mathcal{O}(T)$	$\mathcal{O}(T)$
CSI-based (AO) algorithm [22]	$\mathcal{O}(N)$	$\mathcal{O}(M^3 + N^{3.5})$

in the proposed scheme. Here, we consider the benchmark scheme that estimates N cascaded channels by sending N pilot symbols while changing the RIS activation patterns. The comparisons are listed in Table I.

In the proposed scheme, the RIS pattern optimization is carried out every T pilot transmission, while the conventional scheme typically requires N full pilot transmissions. Hence, in the proposed scheme, decreasing the T value contributes to the reduction of the pilot overhead and the delay, which are imposed by the RIS pattern control. By contrast, in the conventional CSI-based RIS control, non-convex optimization is carried out based on the estimated CSI. However, since the original rate-maximization problem of an RIS-assisted communication scenario is typically non-convex, obtaining the optimal solution is a challenging task [21]. Also, even in the sub-optimal solution based on alternating optimization [22], it imposes the complexity order of $\mathcal{O}(M^3 + N^{3.5})$.

Furthermore, note that pilot symbols are inserted within every coherent interval in the conventional scheme, the associated pilot overhead, delay, and complexity increase upon increasing the channel's time variation.

III. PERFORMANCE RESULTS

In this section, we provide our performance results to demonstrate the achievable performance of the proposed scheme. The conventional full-RIS optimization based on pilot-assisted CSI estimation is employed as a benchmark. The basic system parameters are selected as follows. A carrier frequency and a symbol rate are set to 30 GHz and 120 kHz, respectively. The RIS is placed horizontally on the x -axis from point (5, 5, 0) m. The ULA at the BS is equipped with $M = 8$ antenna elements, which are placed along the x -axis from the origin point. We assume that the user is randomly located within a semicircle with a radius of $\sqrt{50}$ m from the RIS. Large-scale fading coefficients are given by

$$L_{BR} = \xi_0(d_{BR}/d_0)^{\gamma_{BR}} \quad (29)$$

$$L_{RU} = \xi_0(d_{RU}/d_0)^{\gamma_{RU}}, \quad (30)$$

where d_{BR} and d_{RU} denote the distance between the BS and the RIS and that between the RIS and the user while ξ is a reference gain normalized for the distance of $d_0 = 1$ m. Note that, in this paper, the average SNR is defined as [6]

$$\text{SNR} = \frac{P_t L_{BR} L_{RU} N^2 M}{\sigma^2}, \quad (31)$$

where P_t is the transmit power at the BS. In our simulations, we employed $\xi_0 = -62$ dB, $\gamma_{BR} = -2.3$, $\gamma_{RU} = -2$, and $\sigma^2 = -105$ dBm.

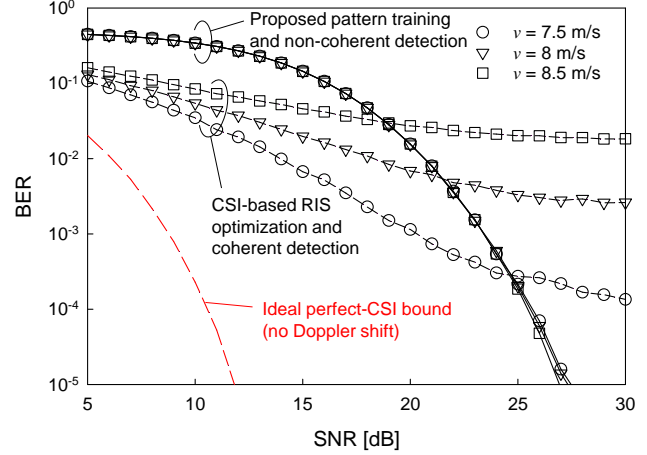


Fig. 2. BER comparisons between the proposed scheme and the benchmark schemes. We consider the system parameters of $(N, T) = (16, 4)$, and the Rice factor of each link is set to $\kappa_{BR} = \kappa_{RU} = 10$ dB. The velocity of the UE is given by $v = 7.5, 8$, and 8.5 m/s.

Fig. 2 shows the achievable BER performance of the proposed and benchmark schemes, where v is varied from 7.5 to 8.5 m/s, while we have the system parameters of $(N, T) = (16, 4)$. Also, we consider $\kappa_{BR} = \kappa_{RU} = 10$ dB. We also plotted the idealistic bound with no Doppler shift, where perfect CSI is used for the RIS optimization and coherent detection. For the benchmark scheme, the block length is set to 34, and 16 pilot symbols are inserted at the beginning of each block. Observe in Fig. 2 that regardless of the v value, the proposed scheme achieved successful error-floor-free curves. By contrast, the benchmark scheme suffers from the error floor, whose level increases upon increasing v due to the effects of the Doppler shift, where the RIS optimization, as well as the coherent detection, is carried out based on the outdated channel estimation. More importantly, the proposed scheme reduced the pilot overhead by a factor of 25% in comparison to the RIS pattern-training scheme.

Fig. 3 shows the BERs of the proposed scheme, where the number of training patterns was given by $T = 2, 4, 8$, and 16, where we have $v = 10$ m/s. Observe in Fig. 3 that the BER performance monotonically improves upon increasing the T value. More specifically, the SNR recorded for the BER of 10^{-4} with $T = 4$ exhibited 6-dB gain over that of $T = 2$. This is because the high number of training patterns allows us to have the high reflected beamforming gain at the sacrifice of increased overhead and delay.

Furthermore, Fig. 4 shows the BERs of the proposed scheme, where the Rice factor was varied from -10 dB to 5 dB, while maintaining $\kappa_{BR} = \kappa_{RU}$. Also, we consider $v = 10$ m/s. It was found that upon increasing the Rice factor, the BER performance improved. This is achieved owing to our system architecture, which is designed for millimeter wave scenarios where the LOS paths are dominant.

Additionally, while our focus in this paper is on a single-user scenario, the proposed scheme is readily applicable to multiuser scenarios, similar to conventional wireless sys-

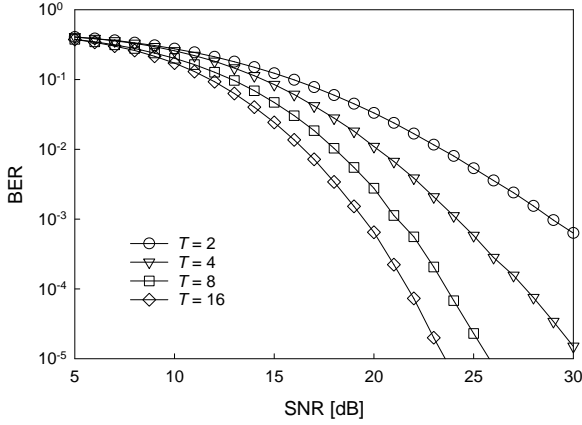


Fig. 3. BER performance of the proposed scheme, where the number of training symbol intervals is given by $T = 2, 4, 8$, and 16 , while we have $N = 16$ and $v = 10$ m/s. The Rice factor of each link is set to $\kappa_{BR} = \kappa_{RU} = 5$ dB.

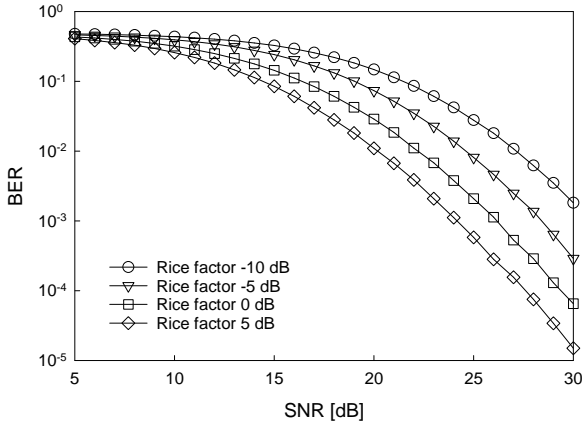


Fig. 4. BER performance of the proposed scheme, where the Rice factor of each link is given by $\kappa_{BR} = \kappa_{RU} = -10$ dB, -5 dB, 0 dB, and 5 dB, while we have $v = 10$ m/s.

tems. For example, our RIS system can be straightforwardly employed in time-division multiple access (TDMA) and frequency-division multiple access (FDMA) scenarios.

IV. CONCLUSIONS

In this paper, we proposed the novel RIS-assisted non-coherent downlink communication scheme. Owing to our amalgamation of CSI-free RIS pattern training and differential coding with noncoherent detection, the RIS control and data communication are accomplished with reduced pilot overhead. Our performance results demonstrated that the proposed scheme outperforms the conventional benchmarks that require channel estimation and non-convex optimization in terms of BER performance.

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